



Leibniz-Institut für Informationsinfrastruktur

Deep Learning, Knowledge Graphs and their Applications

Dr. Mehwish Alam

Workshop on Deep Learning meets Ontologies and Natural Language Processing co-located with FOIS 2020. 16. Sept. 2020

What is a Knowledge Graph?

Google Knowledge Graph

Amith Singhal, Introducing the Knowledge Graph: things, not strings, Google Blog, May 16, 2012

What is a Knowledge Graph?





eb of Data



Google

neil armstrong neil armstrong biography neil armstrong quote neil armstrong timeline

Neil Armstrong

Neil Armstrong - Wikipedia, the free encyclopedia en.wikipedia.org/wiki/Neil Armstrong -

Nell Alden Armstrong (August 5, 1930 - August 25, 2012) was an American astronaut and the first person to walk on the Moon. He was also an aerospace ... Buzz Aldrin - Apollo 11 - Michael Collins - Deism

Neil Armstrong Biography - Facts, Birthday, Life Story - Biography.com



www.biography.com > People * Sep 28, 2011 Learn more about famous astronaut Neil Armstrong military pilot, Korean War veteran, and first man on the ...

More videos for neil armstrong »

Neil Armstrong's 'small step for man' might be a misquote, study say ... www.cnn.com/2013/06/04/tech/armstrong-guote -

Jun 5, 2013 - Neil Armstrong might really have said "one small step for a man," a study finds by lookin at how people speak where he grew up.

Did Neil Armstrong really say, 'That's one small step for a man ...



www.latimes.com/.../la-sci-sn-neil-armstrong-one-small-step-for... * by Karen Kaplan - in 128 Google+ circles

Jun 5, 2013 - Acoustics researchers provide fresh evidence that Nell Armstrong may well have said, 'That's one small step for a man' after landing on the ...

Neil Armstrong - StarChild - NASA

starchild.gsfc.nasa.gov/docs/StarChild/whos who.../armstrong.html * Biography of the test pilot who's first space flight occurred in 1966 aboard Gemini 8.

BBC Solar System - Neil Armstrong facts and rare interviews

www.bbc.co.uk > Science > Space > Solar System > Astronauts + Watch video clips full of facts about Nell Armstrong, the first man on the Moon. See Patrick Moore's rare 1970 interview with Armstrong.

Small Step 'Frrr(uh)' Man: Neil Armstrong's Accent May Have Hid 'a ... www.space.com/21403-neil-armstrong-moon-quote-accent.html * Jun 3, 2013 - Did astronaut Neil Armstrong's famous first words on the moon



Neil Armstrong

Astronaut

Neil Alden Armstrong was an American astronaut and the first person to walk on the Moon. He was also an aerospace engineer, naval aviator, test pilot, and university professor. Wikipedia

Born: August 5, 1930, Wapakoneta, Ohio, United States

Died: August 25, 2012, Cincinnati, Ohio, United States

Space missions: Gemini 8, Apollo 11

Education: University of Southern California (1970), Purdue University (1947-1955), Blume High School (1947)

Spouse: Carol Held Knight (m. 1994-2012), Janet Shearon (m. 1956-1994)

Children: Karen Armstrong, Eric Armstrong, Mark Armstrong

People also search for







Yuri Gagarin

John Glenn

Google Knowledge Graph

70x10⁹ facts 10⁹ entities (03/2017)

structured (meta)data

search recommendations





Artificial Intelligence and Machine Learning



"The Goal of AI is to develop machines that behave as though they were intelligent."

- John McCarthy (1955)



Word2Vec





OUTPUT

Skip-gram

T. Mikolov, I. Sutskever, K. Chen, G. S. Corrado, J. Dean. Distributed representations of words and phrases and their compositionality. NIPS, 2013

Limitations

- Out Of Vocabulary Exceptions (OOV)
- Reason:
 - Internal structure of the word is ignored
 - Problems for **morphologically rich languages** such as Turkish or French etc.
 - In French or Spanish more than 40 different inflections



fastText

- Considers internal structure of the word
- Good for morphologically rich languages
- Based on **skipgram** model with **bag of character n-gram representation** of the words.
- Uses character n-grams as well as the actual words in the scoring function.
- Computes likelihood of each word given a context.

<student>

N = 2 : <st, tu, ud, de, en, nt>

N = 4 : <*stud, tude, uden, dent*>



P. Bojanowski, E. Grave, A. Joulin, T. Mikolov. Enriching Word Vectors with Subword Information. Transactions of the Association for Computational Linguistics, 2017.

Deep Learning for Knowledge Graphs

- NLP and Knowledge Extraction via Deep Learning to populate and extend Knowledge Graphs
- NLP and Knowledge Extraction via Deep Learning for
 Ontology Learning to extend and refine Knowledge Graphs
- NLP and Graph Analysis supported by Deep Learning for Ontology Alignment and Link Discovery to combine and integrate Knowledge Graphs



Graph Representation Learning



- Node Embeddings (Node2Vec, DeepWalk, LINE, etc.) [13]
- Graph Neural Networks: Graph Convolutional Networks [11], Graph Attention Networks, Neural Message Passing, ...
- Knowledge Graph Embeddings: TransE, DistMult, ...

ECAI 2020 Tutorial: Knowledge Graph Embeddings: From Theory to Practice



Knowledge Graph Embedding Techniques

Categories	Without literals	With literals
Translational Distance Models	TransE and its extensions: TransH, TransR, TransD, TranSparse, TransA, etc.	TransEA, DKRL, IKRL, Jointly(desp), Jointly, SSP, KDCoE, EAKGAE
Semantic Matching Models	RESCAL and Its Extensions: DistMult, HoIE, ComplEx, etc. Semantic Matching with Neural Networks: SME, NTN, MLP, etc.	LiteralE, MKBE, MTKGNN, KGlove with literals, Extended RESCAL, LiteralE with blocking
Models using Relation Paths	PTransE, Traversing KGs in Vector Space, RTRANSE, Compositional vector space, Reasoning using RNN, Context-dependent KG embedding.	KBLRN
Models using Temporal Information	Time-Aware Link Prediction, co-evolution of event and KGs, Know-evolve.	
Models using Graph Structures	GAKE, Link Prediction in Multi-relational Graphs.	KBLRN



Translational Distance Model

- Exploit distance-based scoring functions
- Measure the **plausibility of a fact** as the **distance between the two entities**
- A translation carried out by the relation.
- Models: TransE, TransH, TransR, TransD, TransSparse, TransM, TransEdge

Q. Wang, Z. Mao, B. Wang, L. Guo. Knowledge graph embedding: A survey of approaches and applications. IEEE Transactions on Knowledge and Data Engineering (TKDE), 2017.





- Entities and relations are embedded into **same vector space**.
- Consider relation r as translation from entity h to entity t
- Learning Assumption **h+r=t**



Entity and Relation Space

A. Bordes et al. "Translating embeddings for modeling multi-relational data." *Advances in neural information processing systems*. 2013.



TransH

- From original space to Hyperplane
- TransH enables different roles of an entity in different relations.
- Entities h and t are projected into specific hyperplane of relation r.
- Then predict new links based on translation on hyperplane.



Entity and Relation Space

Z. Wang et al. "Knowledge graph embedding by translating on hyperplanes." AAAI, 2014.



TransR

- TransR is similar to TransH.
- Entities h and t are projected into **specific subspace of relation r**.
- Predict new links based on translation in subspace.



Y. Lin et al. "Learning entity and relation embeddings for knowledge graph completion." AAAI, 2015.



Semantic Matching Models

- Exploit similarity-based scoring functions
- Measures *plausibility of facts* by *matching latent semantics of entities and relations*
- Based on Matrix Operation
- Represent relation as a matrix and produce score function by operation on matrix.
- RESCAL, DistMult, HolE, etc.





Methods Using Graph Structures

- Use Contextual information around an entity.
- Walk based methods
- RDF2Vec
 - Word2Vec converts raw text into vector representations
 - RDF2Vec converts a graph into a sequence of nodes and edges
 - Methods:
 - Graph Walks
 - Weisfeiler-Lehman Subtree RDF Graph Kernels

P. Ristoski, H. Paulheim. Rdf2vec: Rdf graph embeddings for data mining. International Semantic Web Conference, 2016.



Graph walks



Generated Sequences:

- Event \rightarrow inheritsFrom \rightarrow Objective Inuence \rightarrow inheritsFrom \rightarrow Transitive Action ...
- Intentionally act \rightarrow inheritsFrom \rightarrow Invasion Scenario \rightarrow subFrameOf \rightarrow
- Conquering ...

20



Weisfeiler-Lehman Subtree RDF Graph Kernels



Generated Sequences:

- $b \rightarrow g \rightarrow j; b \rightarrow g \rightarrow i; b \rightarrow g \rightarrow f; b \rightarrow g \rightarrow h; b \rightarrow g \rightarrow j \rightarrow f$
- $\bullet \quad a {\rightarrow} f {\rightarrow} g; a {\rightarrow} f {\rightarrow} j; a {\rightarrow} f {\rightarrow} i; a {\rightarrow} f {\rightarrow} g {\rightarrow} h$



Applications

- In-KG Applications:
 - Link Prediction: *head, tail, relation prediction*
 - Triple Classification: *Whether unseen triple fact is true or not*
 - Entity Classification: *Classifying entities into different semantic categories*

- Out-KG Applications
 - Relation Extraction
 - Question Answering
 - Recommender System



Libraries for KG Embeddings



https://github.com/facebookresearch/PyTorch-BigGraph

https://github.com/SmartDataAnalytics/PyKEEN

https://github.com/Accenture/AmpliGraph



PyKeen

OpenKE

http://openke.thunlp.org/



What about literals?



Why Literals for KG Embedding?





Why Literals for KG Embedding?





Why Literals for KG Embedding?



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Types of Literals

- Text Literals
 - Short text

fb:m.03vdmh fb:type.object.name "Photo-essay"@en.

• Long text:

fb:m.03vdmh fb:common.topic.description "A photo-essay is a set or series of photographs that are intended to tell a story or ..."@en.

• Numerics Literals

fb:g.1269m_vlb fb:people.person.date_of_birth
"1957"^^<<u>http://www.w3.org/2001/XMLSchema#gYear</u>> .
fb:m.064r8g fb:people.person.weight kg "102.0" .

• **Others:** Images, audio files, video files, and etc.

@prefix fb: <http://rdf.freebase.com/ns/>



KG Embedding Models with Text Literals

- Extended RESCAL Tensor factorization
- Description-Embodied Knowledge Representation Learning (DKRL) TransE + CBOW/CNN
- Multilingual KG Embeddings for cross-lingual KG alignment (KDCoE) TransE + AGRU for multilingual KGs

Drawback: Don't consider short text!!



KG Embedding Models with Numeric Literals

- Multi-Task Knowledge Graph Neural Network (MT-KGNN)
 Regression, Binary Classification
- Knowledge Base Representations with Latent, Relational, and Numerical Features (KBLRN) *TransE, Probabilistic Product of Experts*
- LiteralE

Learnable transformation function

• TransEA

TransE, Linear Regression

Drawbacks:

- Units and data types of literals are not interpreted
- Multi-valued literals are not treated.



Other kind of literals

- Image Literals: IKRL, MTKGRL
- Multi-modal Liaterls:
 - Numeric & Text Literals: LiteralE with blocking, EAKGAE.
 - Numeric, Text & Image Literals: MKBE
- Evaluation Tasks:
 - Link Prediction: *head, tail, relation prediction*
 - Triple Classification: *Whether unseen triple fact is true or not*
 - Entity Classification: *Classifying entities into different semantic categories*



Applications

	Link prediction	Triple Classif.	Entity Classif.	Entity Alignment	Attribute Value Prediction	Nearest Neighbor Analysis	Data Linking	Document classification
Extended RESCAL	V							
LiteralE	V					V		
TransEA	V							
KBLRN	V							
DKRL	V		V					
KDCoE	V			\checkmark				
KGlove with literals		V						\checkmark
IKRL	V	V						
EAKGE	V			V				
MKBE	V				V			
MT-KGNN		\checkmark			\checkmark			
LiteralE with blocking								
							Karkruhar lostitu	t für Tachnologia



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Limitations



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Results for Link Prediction on FB15K-237

	Da	atasets
	FB15K	FB15K-237
Entities	14951	14541
Object Relations	1345	237
Data Relations	118	118
Relational Triplets	592213	310116
Train sets	483142	272115
Valid sets	50000	17535
Test sets	59071	20466

Tail Prediction							
Models	MR	MRR	Hits@1	Hits@3	Hits@10		
$DistMult-LiteralE_{g_{lin}}$	426	0.195	0.119	0.214	0.349		
ComplEx-Literal $E_{g_{lin}}$	575	0.17	0.104	0.185	0.306		
ConvE-LiteralEglin	362	0.187	0.112	0.204	0.338		
DistMult-LiteralEg	359	0.215	0.137	0.234	0.371		
$ComplEx-LiteralE_g$	493	0.175	0.106	0.19	0.312		
ConvE-LiteralEg	459	0.131	0.07	0.137	0.256		
KBLN	501	0.207	0.128	0.23	0.362		
MTKGNN	580	0.191	0.12	0.208	0.338		
TransEA	203	0.206	0.25	0.409	0.57		

Head Prediction								
Models	MR	MRR	Hits@1	Hits@3	Hits@10			
DistMult-LiteralE g_{lin}	245	0.377	0.279	0.422	0.568			
ComplEx-Literal $E_{g_{lin}}$	371	0.36	0.271	0.4	0.538			
ConvE-LiteralEglin	208	0.388	0.296	0.427	0.572			
DistMult-LiteralEg	209	0.413	0.320	0.456	0.591			
$ComplEx-LiteralE_g$	315	0.366	0.277	0.404	0.543			
ConvE-LiteralEg	236	0.317	0.229	0.345	0.501			
KBLN	381	0.386	0.295	0.426	0.564			
MTKGNN	437	0.383	0.295	0.423	0.559			
TransEA	389	0.111	0.094	0.197	0.342			

Both Head and Tail Prediction

Models	MR	MRR	Hits@1	Hits@3	Hits@10
DistMult-LiteralEglin	335	0.286	0.199	0.318	0.458
$ComplEx-LiteralE_{g_{lin}}$	473	0.265	0.187	0.292	0.422
ConvE-Literal $E_{g_{lin}}$	285	0.287	0.204	0.315	0.455
DistMult-LiteralEg	284	0.314	0.228	0.345	0.481
$ComplEx-LiteralE_g$	404	0.27	0.191	0.297	0.427
ConvE-LiteralEg	347	0.224	0.149	0.241	0.378
KBLN	441	0.296	0.211	0.328	0.463
MTKGNN	508	0.287	0.207	0.315	0.448
TransEA	296	0.158	0.172	0.303	0.456

0.456 **FIZ Karlsruhe** Leibniz-Institut für Informationsinfrastruktur

G. A. Gesese, R. Biswas, M. Alam, H. Sack. A Survey on Knowledge Graph Embeddings with Literals: Which model links better Literal-ly?. *Semantic Web Journal (Accepted), 2020.*

Knowledge Graph Embeddings for Downstream Tasks



Event-based Knowledge Reconciliation using Frame Embeddings and Frame Similarity



Knowledge Reconciliation



Why Knowledge Reconciliation:

- Text Summarization
- Document Similarity
- Generating Textual Analytics

Existing Tool MERGILO

- Graph Compression
- Graph Alignment
- Uses String matching and Word Similarit,



M. Alam, D. R. Recupero, M. Mongiovi, A. Gangemi, P. Ristoski. Event-based knowledge reconciliation using frame embeddings and frame similarity. *Knowledge-Based Systems*, 2017.

FRED - Event Oriented Knowledge Graphs from Text

Spaniards attacked the Incas



Semantic Web Machine Reading with FRED. Semantic Web Journal, 2017.

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Framester



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A. Gangemi, M. Alam, L. Asprino, V. Presutti, D.R. Recupero. Framester: A Wide Coverage Linguistic Linked Data Hub. *EKAW*, 2020.

Applications Using Knowledge Graph Embeddings



Reconciled Knowledge Graph





Cross-document Coreference Resolution (CCR) on RDF

		muc	bcub	ceafm	blanc	ceafe
MERGILO Ba	aseline	24.05	17.36	28.61	10.70	26.20
	FrameNet In	heritance	Similarit	y Measure	ès	
Wu-Palmer		27.14	19.91	31.91	12.81	29.41
Path		27.16	19.93	31.85	12.73	29.38
Leacock Choo	dorow	27.04	19.80	31.74	12.77	29.21
	Graph walks	(full frar	ne and ro	le graphs)	
Frame2Vec	Role2Vec	muc	muc bcub ceaf			ceafe
CBOW_200	CBOW_200	27.34	19.99	32.15	12.66	29.82
CBOW_200	SG_800	27.38	19.97	32.29	12.69	29.98
CBOW_200	SG_500	27.28	19.95	31.99	12.69	29.54
	Graph kernels	s (full fra	me and r	ole graphs	5)	
Frame2Vec Role2Vec muc bcub ceafm b				blanc	ceafe	
CBOW_200	SG_200	26.70	19.52	31.45	12.40	28.99
CBOW_200	SG_500	26.70	19.52	31.45	12.40	28.99
SG_200	CBOW_200	26.86	19.62	31.67	12.48	29.18
SG_500	CBOW_200	26.90	19.68	31.58	12.60	29.08



Weakly Supervised Short Text Categorization Using World Knowledge



Where do we find short-text?



Social Media

News Articles

Chatbot



Why short-text classification is challenging?



"Floyd revolutionized rock with the Wall."

Ambiguity! Lack of contextual information!

Humans transfer knowledge from other similar situations or external resources.

Contextual Information is required for understanding.



Explicit Representation

Explicit representation refers to the conceptualization [1].

<u>Floyd</u> revolutionized <u>rock</u> with the <u>Wall</u>.

https://en.wikipedia.org/wiki/Pink_Floyd

https://en.wikipedia.org/wiki/Defensive wall https://en.wikipedia.org/wiki/Berlin Wall https://en.wikipedia.org/wiki/The Wall

https://en.wikipedia.org/wiki/Rock_(geology) https://en.wikipedia.org/wiki/Rock_music https://en.wikipedia.org/wiki/Dwayne_Johnson



Wide & Deep Model for Short Text Classification



R. Türker, L. Zhang, M. Alam, H. Sack. Weakly Supervised Short Text Categorization Using World Knowledge. *International Semantic Web Conference, 2020.*

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Classification Accuracy

Model	Feature	AG News	Snippets	DBpedia	Twitter
Wide	Entity Co-occurance (Ent Co)	0.561	0.447	0.499	0.278
	Text	0.802	0.795	0.786	0.555
	Entity	0.790	0.764	0.775	0.521
	Category	0.773	0.698	0.754	0.444
Deep	Text+Entity	0.793	0.785	0.779	0.524
Deep	Text+Category	0.801	0.794	0.786	0.554
	Entity+Category	0.792	0.771	0.771	0.534
	Text+Entity+Category	0.792	0.786	0.785	0.529
	Ent Co+Text	0.807	0.792	0.786	0.556
	Ent Co+Entity	0.791	0.774	0.768	0.520
	Ent Co+Category	0.792	0.693	0.774	0.446
Wide & Deep	Ent Co+Text+Entity	0.787	0.802	0.776	0.53
	Ent Co+Text+Category	0.814	0.803	0.792	0.581
	Ent Co+Entity+Category	0.791	0.770	0.766	0.544
	Ent Co+Text+Entity+Category	0.790	0.805	0.778	0.572



Knowledge Graph Embeddings based Type Prediction



Motivation

What are the types of the following entities?



Instrument





R. Biswas, R. Soforonova, M. Alam, H. Sack. Entity Type Prediction in Knowledge Graphs using Embeddings. *DL4KG@ESWC, 2020*.

Motivation

What are the types of the following entities?



Pipeline of the Unsupervised Approach

Unsupervised approach is based on the vector similarity between the class vector and entity vector





Supervised Approach - 1D CNN



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Wrapping Up

- What did we see so far:
 - Knowledge Graphs
 - Graph Neural Networks
 - Knowledge Graph Embeddings with or without Literals
 - Downstream tasks using Knowledge Graph Embeddings

• What next?

- Temporal Knowledge Graph Embeddings
- More expressivity
- Explainability in Knowledge Graph Embeddings



Some Advertisements



Special Issue in Deep Learning and Knowledge Graphs

Call for papers: Special Issue on Deep Learning and Knowledge Graphs

Submitted by Pascal Hitzler on 07/04/2020 - 05:29

Call for papers: Special Issue on

Deep Learning and Knowledge Graphs

Over the past years there has been a rapid growth in the use and the importance of Knowledge Graphs (KGs) along with their application to many important tasks. KGs are large networks of real-world entities described in terms of their semantic types and their relationships to each other. On the other hand, Deep Learning has also become an important area of research, achieving important breakthroughs in various research fields, especially Natural Language Processing (NLP) and Image Processing. Moreover, in recent years Deep Learning methods have been combined with KGs. For example: 1) knowledge representation learning techniques aimed at embedding entities and relations in a KG into a dense and low-dimensional semantic space, 2) relation extraction techniques, aimed at extracting facts and relations from text and needed to construct KGs, 3) entity linking techniques, aimed at completing KGs, 4) using KGs as an additional prior for image recognition, etc.

In order to pursue more advanced methodologies, it has become critical that the communities related to Deep Learning, Knowledge Graphs, and NLP join their forces in order to develop more effective algorithms and applications. This special issue aims to reinforce the relationships between these communities and foster interdisciplinary research in the areas of KG, Deep Learning, and Natural Language Processing.

Topics of Interest

- New approaches for the combination of Deep Learning and Knowledge Graphs
 - Methods for generating Knowledge Graph (node) embeddings
 - Scalability issues
 - Temporal Knowledge Graph Embeddings
 - Novel approaches



https://tinyurl.com/yyzeok6l



Join us!!



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